

Accelerated Precalculus
Bearings Practice

Name _____
Period _____ Date _____

Sketch each of the following and find the magnitude and bearing of each resultant.

1. A plane flies $N38^\circ E$ for 300 miles, develops engine trouble and changes course to $S71^\circ E$ for 30 miles to land at the nearest airport.
2. A ship travels 1500 km heading 36° west of south, then changes course to travel 4000 km on a heading of 78° west of south.
3. On a treasure hunt, Sally walks 30 ft on a bearing of $N56^\circ W$, then turns and walks $N10^\circ E$ for another 45 ft.
4. A jet flies 600 km heading 65° east of north, has a medical emergency and changes course to find an airport 40 km 10° west of south.

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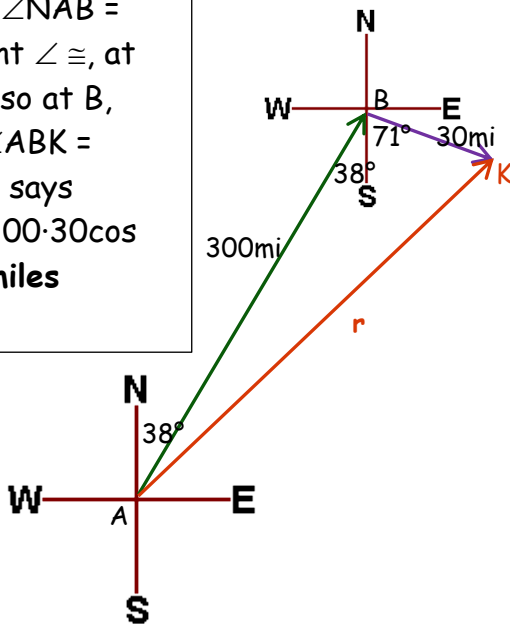
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Sketch each of the following and find the magnitude and bearing of each resultant.

1. A plane flies $N38^\circ E$ for 300 miles, develops engine trouble and changes course to $S71^\circ E$ for 30 miles to land at the nearest airport. The initial path is in green and the next is in purple. The resultant is in orange.

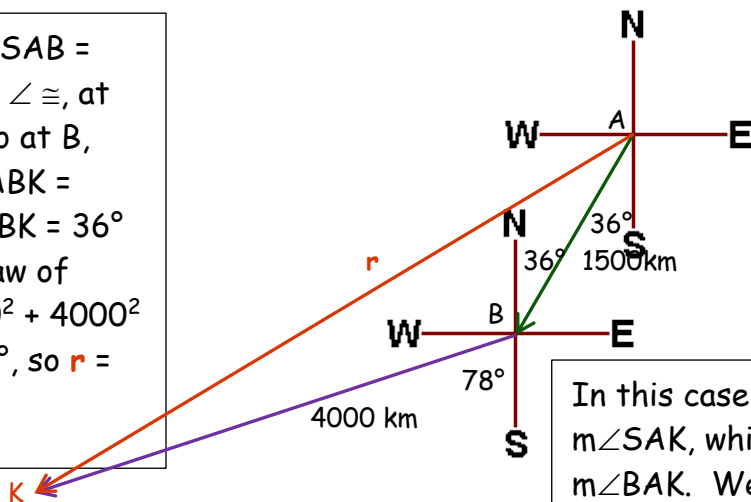
Notice that at A, $m\angle NAB = 38^\circ$. Since $\parallel \rightarrow$ alt. int $\angle \cong$, at B, $m\angle ABS = 38^\circ$. Also at B, $m\angle SBK = 71^\circ$, so $m\angle ABK = 109^\circ$. Law of cosines says $r^2 = 300^2 + 30^2 - 2 \cdot 300 \cdot 30 \cos 109^\circ$, so $r = 311.1$ miles



The bearing is sometimes more of a challenge because you must stop and find the angle made from the north or south and the resultant. This usually involves adding or subtracting angles. In this case, we need $m\angle NAK$, which is $38^\circ + m\angle BAK$. We find $m\angle BAK$ using the law of sines: $r/\sin 109^\circ = 30/\sin \angle BAK$. So $m\angle BAK = 5.232^\circ$. (I used saved values for r.) So the bearing is $N43.232^\circ E$.

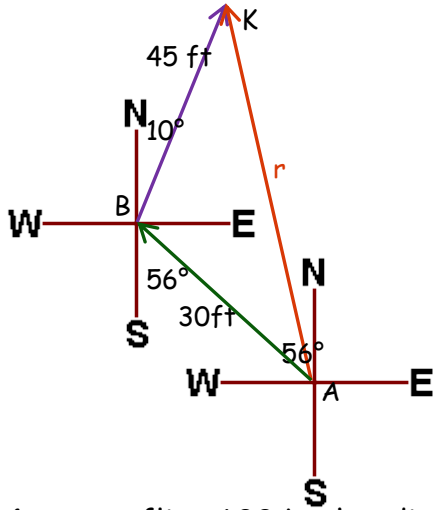
2. A ship travels 1500 km heading 36° west of south, then changes course to travel 4000 km on a heading of 78° west of south.

Notice that at A, $m\angle SAB = 36^\circ$. Since $\parallel \rightarrow$ alt. int $\angle \cong$, at B, $m\angle ABN = 36^\circ$. Also at B, $m\angle SBK = 78^\circ$, so $m\angle ABK = m\angle ABN + 90^\circ + m\angle WBK = 36^\circ + 90^\circ + 12^\circ = 138^\circ$. Law of cosines says $r^2 = 1500^2 + 4000^2 - 2 \cdot 1500 \cdot 4000 \cos 138^\circ$, so $r = 5212$ km



In this case, we need $m\angle SAK$, which is $36^\circ + m\angle BAK$. We find $m\angle BAK$ using the law of sines: $r/\sin 138^\circ = 4000/\sin \angle BAK$. So $m\angle BAK = 30.90^\circ$. So the bearing is $S66.90^\circ W$.

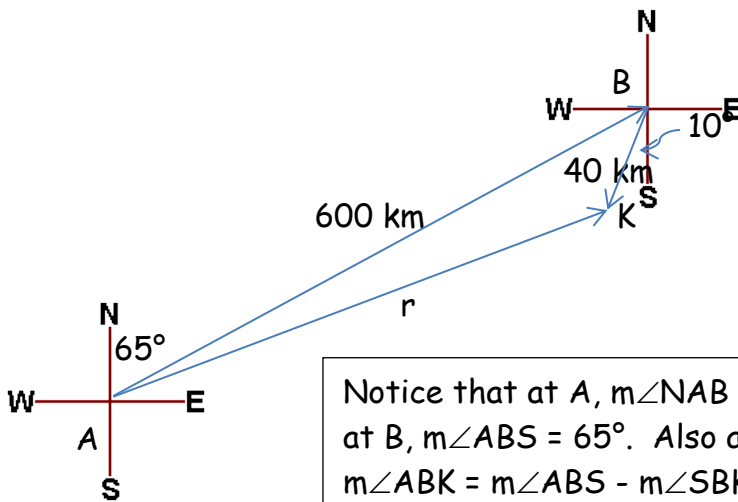
3. On a treasure hunt, Sally walks 30 ft on a bearing of N56°W, then turns and walks N10°E for another 45 ft.



Notice that at A, $m\angle NAB = 56^\circ$. Since $\parallel \rightarrow$ alt. int $\angle \cong$, at B, $m\angle ABS = 56^\circ$. Also at B, $m\angle NBK = 10^\circ$, so $m\angle ABK = 180^\circ - m\angle ABS - m\angle NBK = 180^\circ - 56^\circ - 10^\circ = 114^\circ$. Law of cosines says $r^2 = 30^2 + 45^2 - 2 \cdot 30 \cdot 45 \cos 114^\circ$, so $r = 63.43$ ft.

In this case, we need $m\angle NAK$, which is $56^\circ - m\angle BAK$. We find $m\angle BAK$ using the law of sines: $r/\sin 114^\circ = 45/\sin \angle BAK$. So $m\angle BAK = 40.40^\circ$. So the bearing is **N15.60°W**.

4. A jet flies 600 km heading 65° east of north, has a medical emergency and changes course to find an airport 40 km 10° west of south.



Notice that at A, $m\angle NAB = 65^\circ$. Since $\parallel \rightarrow$ alt. int $\angle \cong$, at B, $m\angle ABS = 65^\circ$. Also at B, $m\angle SBK = 10^\circ$, so $m\angle ABK = m\angle ABS - m\angle SBK = 65^\circ - 10^\circ = 55^\circ$. Law of cosines says $r^2 = 600^2 + 40^2 - 2 \cdot 40 \cdot 600 \cos 55^\circ$, so $r = 578.0$ ft.

In this case, we need $m\angle NAK$, which is $65^\circ + m\angle BAK$. We find $m\angle BAK$ using the law of sines: $r/\sin 55^\circ = 40/\sin \angle BAK$. So $m\angle BAK = 3.250^\circ$. So the bearing is **N68.25°W**.